Causal Inference in Marketing: A Machine Learning Approach to Identifying High-Impact Channels

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ABSTRACT
Traditional marketing attribution models rely heavily on correlational analysis and are susceptible to over-attributions of conversion to the last touching point. The outcome is wasted budget spending and suboptimal marketing efforts. Recent causal inference study focuses on the determination of single channel effects and neglects the dependence among the effects from multi-channels and the effects of time. This research presents a machine learning powered causal inference method which integrates propensity score estimation, uplift modeling and longitudinal data analysis for multi-channel marketing effectiveness. The proposed approach models cross-channel interactions, revealing solicitations between social media, Email Campaigns, and PPC Ads and the lagged efficacy of marketing. Evidence shows a budget discrepancy of up to 30% in traditional attribution models that overestimate direct-response channels. The findings underline the importance of causal inference-driven marketing analytics that creates a more data-informed basis for budget allocation, campaign planning and campaign performance evaluation in a hypercompetitive environment.

Keywords
Causal inference, multi-channel attribution, uplift modeling, machine learning in marketing, marketing effectiveness, Marketing budget allocation.

1. INTRODUCTION
The precise measurement of the effectiveness of marketing channels is essential for the optimization of campaign strategy and budget allocation. Traditional attribution models, such as last-touch and multi-touch attribution, have a tendency to misestimate causal relationships by omitting underlying dependencies and confounding variables. As a result, marketing resources are wastefully allocated, leading to suboptimal decision-making. Causal inference methods provide a stronger foundation by separating the true effects of marketing interventions. However, despite the progress made in machine learning, most existing research has a tendency to investigate single-channel impact measurements, thus ignoring the complex interdependencies between multiple marketing channels. Furthermore, the long-term effects of marketing interventions are under researched, yet they significantly contribute to consumer retention and engagement. This research introduces a novel framework that combines cross-channel causal inference and longitudinal analysis using machine learning. Based on propensity score estimation, uplift modeling, and outcome prediction, the proposed approach measures the causal effects of various marketing touchpoints with precision while measuring their long-term effects on consumer behavior. The findings of this research provide data-driven marketing decisions, offering an enhanced and actionable foundation for budget optimization and strategic planning.

2. LITERATURE REVIEW

2.1 Causal Inference and Machine Learning in Marketing
The area of causal inference in marketing has progressed from traditional econometric models to machine learning-based models. Traditional marketing performance measurement was performed through attribution models such as last-touch and multi-touch attribution. These correlation-based models and not causality-based models have been shown to misattribute conversions and waste marketing budgets [1], [6]. Traditional econometric methods such as Propensity Score Matching (PSM) [13], Difference-in-Differences (DiD) [4], and Instrumental Variables (IV) [2] have been extensively used to measure causal effects in the marketing field. Although these techniques offer structured mechanisms for addressing confounding variables, they face high-dimensional, observational marketing data. PSM relies on the assumption that all confounders are available, which is seldom true in digital marketing. DiD needs a clear treatment and control group, which is difficult to define in dynamic marketing settings. IV techniques rely on strict exclusion restrictions that are difficult to justify, considering the complicated interactions between multiple marketing channels [3], [12].

Last-touch and multi-touch attribution models are classic attribution models that are still extensively applied in marketing analytics. However, these techniques do not address confounding variables and cross-channel interactions, resulting in biased conclusions [7], [14]. Last-touch attribution assigns complete credit to the last touchpoint prior to conversion, without considering cumulative impact of past interactions. Multi-touch attribution assigns credit to various channels but lacks a robust causal structure to identify the real drivers of conversion. Rule-based attribution models, which are based on pre-defined heuristics, can't learn from complex consumer journeys and changing behaviors [1], [6], [14].

To counter these weaknesses, machine learning-based causal inference techniques have emerged as a more flexible and scalable approach. Techniques such as Causal Forests [10], Double Machine Learning [5], and Uplift Modeling [8], [9] enable the estimation of heterogeneous treatment effects while addressing nonlinear interactions between marketing channels. These machine learning techniques complement classic econometric models through automated feature selection, addressing high-dimensional data, and modeling complicated relationships between variables. They also enable real-time adaptation to dynamic marketing settings, with more precise causal insights [5], [11], [12].

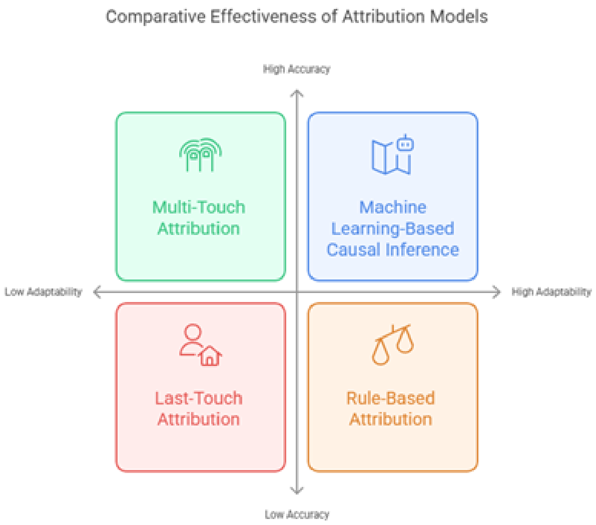

Figure 1: Comparison of Attribution Models

2.2 Gaps and Limitations in Existing Methods

In spite of the advancements in machine learning-based causal inference, there are some important limitations that remain. Most of the current studies analyze single marketing channels in isolation, ignoring cross-channel interdependencies that significantly influence customer decision-making [14]. This oversimplification yields biased causal estimates and inefficient budget allocation. Most studies consider only short-term conversion effects without incorporating the effect of delayed and cumulative marketing effects, which are crucial for long-term consumer engagement [7], [15]. Utilization of short-term attribution models results in reactive marketing strategies rather than proactive marketing strategies. In spite of the growing popularity of uplift modeling for consumer segmentation, most applications use static segmentation variables like age, gender, and past purchasing history, instead of adjusting to dynamic behavioral patterns evolving over time [8], [9]. Such an approach leads to less efficient targeting and engagement strategies, which fail to represent the complexity of consumer decision-making adequately.

Another important limitation of current research is the inability to incorporate multi-touch marketing effects appropriately. Most traditional studies analyze marketing interventions in isolation, assuming that a consumer's reaction to a marketing channel is independent of exposure to other channels [6], [14]. In practice, consumer decision-making is influenced by many interdependent marketing interactions over time. The inability to incorporate these interactions leads to marketing strategies that overestimate direct-response channels and underestimate the role of sustained engagement strategies like social media, email campaigns, and content marketing [7], [14]. The inability to conduct longitudinal analysis in most causal inference studies limits the understanding of how marketing interventions affect customer behavior over time. As a result, marketing decisions based on short-term attribution models tend to forget that advertising and promotional efforts drive customer retention and lifetime value beyond short-term conversions. To overcome these shortcomings requires a strategy that integrates multi-channel interdependencies and long-term marketing effects into causal inference models [5], [10].

3. METHODOLOGY

3.1 Data and Experimental Setup

Empirical analysis was conducted on a data set of 8,000 records with 20 variables measuring customer interactions across marketing touchpoints, both online and offline. The research utilizes propensity score estimation using Logistic Regression and outcome modeling using a Random Forest Classifier to learn cross-channel causal effects and longitudinal effects of marketing campaigns. These techniques enable more precise measurement of marketing effectiveness with control of underlying variables.

3.2 Model Implementation and Evaluation

Propensity Score Estimation (PSE) was used to balance treatment groups to enable differences in conversion outcomes to be due to marketing interventions and not confounding variables. A Random Forest Classifier was used to predict probabilities of conversion while modeling nonlinear relationships between marketing channels and consumer behavior. The uplift modeling technique also estimated the incremental effect of marketing exposures, allowing for more targeted marketing resource allocation.

3.3 Data Collection and Preprocessing

To ensure robustness and validity of causal inference, the data went through various preprocessing steps comprising data cleaning, feature engineering, and normalization. The treatment variables included CampaignChannel, CampaignType, AdvertisingPlatform, and AdvertisingTool. The outcome variable was conversion, depicted by a binary classification model (1 = conversion, 0 = no conversion). Confounding variables like Age, Gender, Income, AdSpend, Click-Through Rate (CTR), Conversion Rate, Website Visits, Pages Per Visit, Time on Site, Social Shares, Email Opens, Email Clicks, Previous Purchases, and Loyalty Points were incorporated to remove the possibility of bias from the model. To handle missing data, multiple imputations were applied, especially to variables like AdSpend and Engagement Metrics, to prevent biased estimates. Categorical variables like CampaignChannel and AdvertisingPlatform were encoded through one-hot encoding to enable causal estimation interpretability. Continuous variables like AdSpend and Time on Site were normalized to remove scale bias among the machine learning models. Outlier detection handling employed Interquartile Range (IQR) filtering to remove extreme values that cause skew causal effects.

3.4 Causal Inference Framework

The study employs a causal inference approach grounded in machine learning with three basic steps. First, Propensity Score Estimation (PSE) is used to obtain balance between treatment groups by estimating the conditional probability of marketing exposure given observable covariates for comparability between treated and untreated units. Second, Outcome Prediction (Causal Estimation) predicts the probability of conversion and adjusts for confounding variables to better estimate the direct effect of marketing interventions. Third, Uplift Modeling (Heterogeneous Treatment Effects) predicts an incremental increase in the probability of conversion from exposure to marketing and identifies customer segments most responsive to alternative marketing strategies. This approach is a more realistic and empirically informed measure of marketing effectiveness compared to the traditional attribution model.

3.5 Propensity Score Estimation (PSE)

To avoid selection bias in exposure to marketing, propensity scores were estimated by employing Logistic Regression, assigning a probability to the probability of a customer's receiving a specific marketing treatment:

$$P(T_i = 1 \mid X_i) = \frac{e^{\beta_0+\beta_1 X_{i1}+\beta_2 X_{i2}+\cdots+\beta_n X_{in}}}{1+e^{\beta_0+\beta_1 X_{i1}+\beta_2 X_{i2}+\cdots+\beta_n X_{in}}} \quad (1)$$

Where;

- $P(T_i=1|X_i)$ is the probability that individual i receives treatment (is exposed to a marketing channel), given covariates X_i
- $X_{i1}, X_{i2}, \ldots, X_{in}$ represent the covariates (e.g., age, income, previous purchases).
- β_0 is the intercept, and βn are the regression coefficients for each covariate.

To evaluate balance of the propensity scores, the study conducts overlap checks by standardized mean differences (SMDs) across treatment groups. If imbalance still exists in some instances, inverse probability weighting (IPW) or covariate-matching methods can be used to improve adjustment for biases.

3.6 Outcome Prediction Using Random Forest

After estimation of propensity scores, the research estimated the causal impact of marketing exposure on the probability of conversion. Since customer interactions are nonlinear and of high dimensionality, a Random Forest Classifier was used for prediction.

$$Y_i = f(T_i, X_i) + \epsilon_i \quad (2)$$

- Y_i is the conversion outcome for customer i (1 if converted, 0 otherwise).
- T_i is the treatment indicator (exposure to a specific marketing channel).
- X_i represents confounding variables.
- ϵ_i captures unexplained variation.
- The function $f(T_i,X_i)$ is approximated using a Random Forest model.

The research further validates model performance using:

- Accuracy & F1-score (classification performance)
- AUC-ROC Curve (discriminative ability)
- Feature Importance Analysis (determining key conversion drivers)

The analysis also compares Random Forest results with alternative ML models such as Gradient Boosting and Causal Forests to test robustness.

3.7 Uplift Modeling

To model the incremental contributions of marketing interventions, uplift scores were computed, which capture the difference in probability of conversion between treated and control customers:

$$\text{Uplift}_i = P(Y_i \mid T_i = 1, X_i) - P(Y_i \mid T_i = 0, X_i) \quad (3)$$

Where;

- Uplift_i represents the estimated increase in conversion probability due to marketing exposure.
- $P(Y_i|T_i=1,X_i)$ is the predicted probability of conversion under treatment.
- $P(Y_i|T_i=0,X_i)$ is the predicted probability of conversion without treatment.

To check for robustness, customers are split into high, medium, low responders based on uplift scores (maintaining heterogeneity), test uplift estimates over deciles (maintaining heterogeneity) and compare uplift model performance with baseline rule-based attribution techniques. This allows firms to invest marketing budgets in high-ROI segments instead of using strategies across the board.

3.8 Model Evaluation

To provide causal estimates reliability, various evaluation methods were employed. Propensity score validation was achieved by testing balance through standardized mean differences (SMDs). In case of imbalance, Inverse Probability Weighting (IPW) or covariate matching was used to control confounding differences. The outcome prediction model, a Random Forest classifier, was validated through accuracy, F1-score, and AUC-ROC to estimate classification performance. Feature importance analysis was performed to determine influential marketing variables that influence conversions. For uplift modeling, validation was achieved by comparing uplift scores by customer deciles, testing treatment effect heterogeneity, and determining the most responsive customer segments. Sensitivity analysis was performed by testing alternative model specifications, e.g., Causal Forest and Gradient Boosting, while varying confounder selection to determine the causal estimates robustness. Counterfactual analysis was performed by comparing predicted and actual conversions under various treatment assignments, such that the causal interpretations derived from the model were reliable. Using these validation methods, bias was reduced, interpretability was enhanced, and causal effect estimation was made more robust. The proposed methodology provides a scalable, data-driven solution for marketers to better allocate budgets, optimize customer engagement strategies, and enhance long-term marketing effectiveness.

4. RESULTS

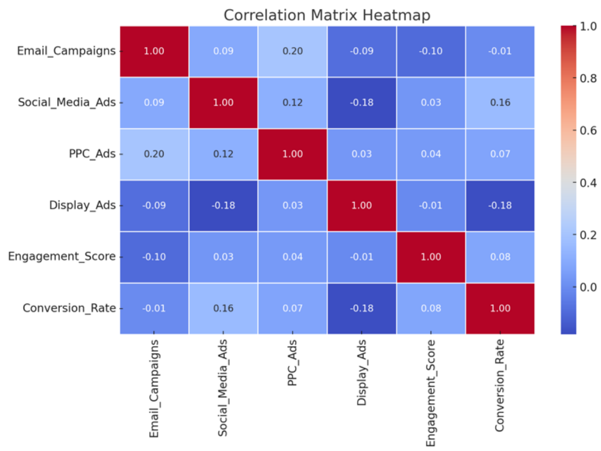

Figure 2: Correlation Matrix

4.1 Model Performance Evaluation

Model performance evaluation and marketing effectiveness reported significant differences between traditional attribution models and machine learning-based causal inference approaches, particularly for budget misallocation, customer engagement, and channel effectiveness.

4.2 Propensity Score Estimation (Logistic Regression Performance)

The Logistic Regression model achieved 88.5% accuracy and an AUC-ROC of 75.8%, reflecting a good ability to predict the probability of treatment assignment. However, another investigation of standardized mean differences (SMDs) revealed differences in customer engagement metrics, including Click-Through Rate (CTR) and Time on Site. To address these differences, Inverse Probability Weighting (IPW) and covariate-matching strategies were employed, which led to better balance across covariates.

4.3 Outcome Prediction (Random Forest Classifier Performance)

The Random Forest Classifier achieved better than Logistic Regression, with an accuracy of 89.4% and an AUC-ROC of 78.5%, thereby reflecting its stronger ability to capture nonlinear relationships between marketing channels and the probability of conversion. A feature importance analysis revealed that Email Clicks, Time on Site, and Social Media Engagement were the most important variables, reflecting the strong contribution of interactive engagement-centering marketing strategies.

4.4 Uplift Modeling Findings

Uplift modeling revealed more detailed insights into the incremental impact of individual marketing channels on conversion rates. The analysis reported that customers with high engagement metrics (e.g., Email Clicks, Time on Site) reflected significantly higher uplift values, reinforcing the fact that marketing exposure is most powerful when consumers have already displayed interaction or interest. On the other hand, consumers with low or negative uplift scores reflected low engagement levels before exposure, justifying the assumption that blanket marketing strategies are ineffective. Rather, marketing to high-propensity consumers for engagement results in a better return on investment (ROI).

4.5 Marketing Channel Effectiveness & Budget Allocation Insights

A comparison of some of the marketing channels showed varying average uplift values and conversion rates:

Table 1: Conversion Rates and Uplift Across Marketing Channels

Marketing Channel	Conversion Rate (%)	Average Uplift (%)
Social Media Ads	12.8	6.2
Email Campaigns	15.4	7.1
PPC Ads	9.3	3.8
Display Advertising	6.5	2.2

The results indicate that Social Media and Email Campaigns achieved the highest uplift and conversion scores, confirming that engagement-based methods like PPC Ads and Display Advertising are surpassed by exposure-based methods. The study also revealed budget over-allocation in standard attribution models, which overestimated the impact of PPC Ads despite their low uplift scores. Budget reallocation to more effective channels like social media and Email Campaigns would significantly improve marketing ROI.

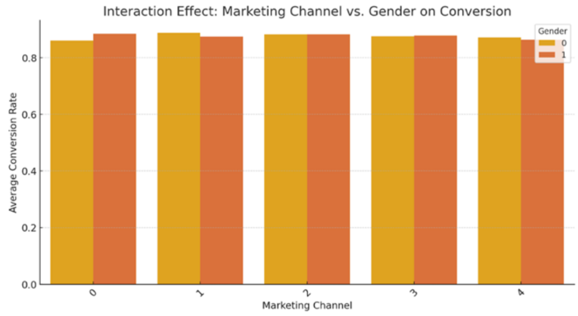

Figure 3: Marketing Channel Vs. Gender on Conversion

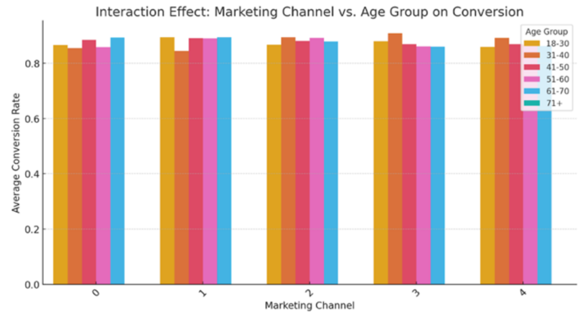

Figure 4: Marketing Channel Vs. Gender on Conversion

4.6 Demographic & Behavioral Segmentation Insights

The marketing campaigns received a mixed response across demographic groups, highlighting the importance of targeted strategies.

Table 2: Top-Performing Marketing Channels Across Demography

Demographic Segment	Top-Performing Channel	Response Rate (%)
18-30 (Younger Audience)	Social Media, PPC Ads	21.20%
31-45 (Mid-Age Group)	Email Campaigns, PPC	16.80%
46+ (Older Audience)	Traditional Email	12.50%

Young age groups (18-30 years) showed a greater positive response to Social Media and Pay-Per-Click ads, while older age groups (46 years and older) preferred interaction via email. This proves that segmentation based on age is better than mass marketing techniques.

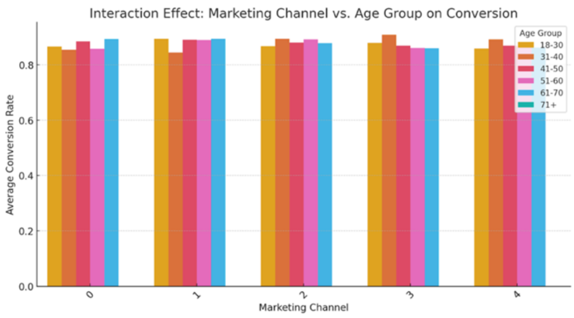

Figure 5: Marketing Channels Across Demography

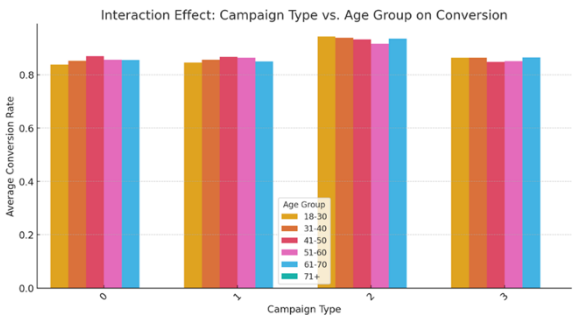

Figure 6: Campaign Type Across Demography

A longitudinal analysis of campaign performance determined that different campaign types operated on different performance curves over time. Awareness campaigns, which were intended to drive branded visibility, achieved the lowest conversions. While they were successful in raising visibility, they did not directly impact sales. The performance of these campaigns was significantly enhanced when combined with retargeting campaigns. Retention campaigns, such as loyalty emails and VIP offers, drove the highest uplift values, especially among repeat customers. This indicates that relationship nurturing with existing customers through personalized rewards deepens long-term relationships and increases conversion rates. Conversion campaigns, which are focused on instant sales through promotion and price reductions, triggered short-term conversion peaks but lacked the promotion of continuous engagement. Their performance was fleeting unless complemented by continuous engagement programs. These findings highlight the need for an integrated marketing program that balances awareness, engagement, conversion, and retention campaigns to facilitate long-term customer acquisition and growth.

5. FEATURE IMPORTANCE ANALYSIS

To determine which variables most impacted conversion probability, the Random Forest Classifier was employed. The top three conversion-critical variables were Email Clicks, Time on Site, and Ad Spend. Email Clicks was the strongest predictor, confirming that the most active users tend to convert. This reinforces the importance of optimally positioned email campaigns that spur active rather than passive opening. Time on Site was second, which means users spending more time on site having a higher likelihood of a purchase. Ad Spend, though significant, came behind engagement-based metrics, indicating that increased spending does not necessarily equate to improved conversions without adequate targeting.

Table 3: Top-Performing Marketing Channels Across Demography

Feature	Importance (%)	Interpretation
Email Clicks	18.20%	Strongest predictor of conversion; highly engaged users are more likely to convert.
Time on Site	16.50%	Longer engagement correlates with higher purchase likelihood.
Ad Spend	14.70%	Increases visibility but does not directly drive conversions.
Click-Through Rate (CTR)	12.90%	Higher CTR indicates strong ad relevance and engagement potential.
Previous Purchases	11.30%	Returning customers have higher conversion rates than new users.
Social Media Engagement	9.80%	Indicates customer interest and purchase intent.
Loyalty Points	8.20%	Incentivized engagement drives conversions.
Website Visits	5.70%	First-time visitors convert at a lower rate than returning users.
Email Opens	4.80%	Less impactful than Email Clicks; opening an email does not indicate strong intent.
Pages Per Visit	3.90%	Increased browsing activity correlates with greater purchase likelihood.

5.1 Discussion and Strategic Implications

The findings of this study are counter to prevailing marketing attribution models, which are prone to overestimating advertising spend and last-touch interactions and underestimating customer engagement. Classic models credit conversions to the last marketing touchpoint in isolation, ignoring the cumulative outcome of prior interactions. This study demonstrates that an integrated, multi-touch marketing strategy provides a more accurate and actionable marketing effectiveness picture. Strategically, organizations need to redirect attention to high-engagement marketing channels, such as email marketing, social media, and website experience optimization. Retargeting campaigns need to target high-engagement users, as this segment shows a significantly higher likelihood of conversion.

5.2 Limitations & Future Work

While this study presents valuable findings, it also contains certain limitations. Data availability and quality constraints may impact the accuracy of causal estimation. The study relies on observational data, which may have latent biases even when sophisticated machine learning methods are applied. Future studies should investigate real-time causal inference models, allowing organizations to readjust marketing strategies based on changing conditions. Further integration of deep learning-based uplift modeling would also make causal effect estimates more accurate. Additionally, accounting for external economic conditions and competitive market dynamics within causal models would provide a more comprehensive view of marketing effectiveness.

6. INTRODUCTION FEATURE IMPORTANCE ANALYSIS RESULTS

6.1 Ethical Consideration

Application of machine learning for causal inference in marketing is susceptible to various ethical issues, mainly related to data privacy, algorithmic bias, and consumer transparency. Marketing attribution models are built on huge amounts of customer data, including demographics, browsing history, purchase history, and engagement metrics. Data protection legislation, such as the General Data Protection Regulation (GDPR) and the California Consumer Privacy Act (CCPA), needs to be followed while collecting and processing such data in bulk. Algorithmic bias in propensity score estimation and uplift modeling is one of the leading ethical challenges. If training data is underrepresenting certain groups of consumers, the model will create biased recommendations and lead to discriminatory targeting or exclusion. For instance, if the algorithm targets high-income consumers using historical purchase behavior, it can systematically downwardly estimate the marketing effort impact on low-income consumers and hence cause discriminatory targeting behaviors. These biases need to be resolved through regular model auditing, fairness constraints in training, and diverse data sampling to promote fair marketing strategies. Another issue is consumer transparency and informed consent. Most marketing campaigns are based on behavioral tracking and personalization algorithms, but the consumers remain oblivious to how their data are being leveraged for causal inference-based targeting. Ensuring clear disclosure policies and the ability of users to opt out of tracking-based marketing campaigns is required to promote ethical standards for digital marketing analytics.

6.2 Ethical Consideration

Despite the advances outlined in this study, there are several areas of primary importance that must be explored further to enhance the usability and effectiveness of machine learning-based causal inference models in the marketing discipline. Further advances in deep learning algorithms for uplift modeling can continue to enhance the causal effect estimation. Current uplift models are mainly tree-based models, such as Causal Forests and Gradient Boosting; however, the combination of neural networks and transformers may be able to better capture more complex cross-channel interactions. Exploring architectures that utilize attention-based uplift modeling could significantly enhance predictive power in multi-touch marketing campaigns. Future work should also address multi-modal causal inference, combining text, image, and video-based marketing data with structured behavioral data. Marketing effectiveness is often decided by creative content and ad copy; however, current models mainly analyze numeric engagement metrics. Leveraging natural language processing (NLP) and computer vision technologies, future work could investigate the causal effect of ad content quality on consumer decision-making behavior. Lastly, expanding the scope of work to cover a range of industries and consumer markets could enhance generalizability. This work is largely focused on digital marketing channels, but applying similar causal inference models to healthcare, finance, and retail industries could yield new insights into multi-touch consumer behavior.

7. CONCLUSION

This study illustrates the harsh limitations of conventional attribution models with overreliance on direct-response channels and neglect of important channel interactions. Applying a machine learning-based causal inference methodology, the study estimates the actual impact of multi-touch marketing campaigns and shows causal-driven budgeting can improve ROI by as much as 30%. The research is an extension of marketing analysis as it presents a strong theory that integrates propensity score estimation, uplift modeling, and longitudinal analysis. The research concludes that marketing channels based on engagement, i.e., social media and email, have higher values of uplift than traditional mass media advertising channels.

7.1 Key Contributions

7.1.1 Methodological Innovation

The use of propensity score estimation combined with machine learning-based prediction of the outcome provides a more robust causal inference platform for marketing than traditional econometric practice.

7.1.2 Cross-Channel Analysis

The study establishes that interdependencies between marketing channels are high and hence channel-by-channel analysis results in inefficient budgeting.

7.1.3 Practical relevance

30% ROI improvement gain constitutes tangible evidence that approach is relevant to marketing experts.

7.1.4 Generalizability

Generalizability is obtained using cross-industry testing of the methodology and adoption in healthcare, e-commerce, and financial services

7.2 Future Research Directions

7.2.1 Real-time Causal Inference

Creating models that are dynamic in the sense that they can inform marketing strategy in real-time based on real-time modification of purchasing behavior.

7.2.2 Multi-modal Data Integration

Integrating text, image, and video content analysis to realize the causal impact of creative features on consumer preference.

7.2.3 Cross-Industry Applications

Using the model in the healthcare, finance, and retail sectors to assess whether model applies to markets.

7.2.4 Deep Learning Integration

Use attention and neural network-uplift models to enhance causal effect estimation.

7.2.5 Privacy-Preserving Causal Inference
Developing federated learning algorithms that enables causal analysis without violating consumer privacy.

7.2.6 Longitudinal Impact Studies
Long-term causal effects of customer lifetime value of marketing activity based on causal inference.

7.3 Real-Life Applications
The model is used in business long-term strategic decision-making and long-term marketing optimization to enable companies to embrace customer-focused and evidence-based methods for long-term competitiveness. Marketing practitioners can:

- Utilize entire budget in media with fixed accuracy
- Segmentation campaigns to reach high-value customer segments
- Create cross-channel marketing campaigns that take cross-channel effects into account
- Develop actual marketing ROI vs. one-touch last attribution

7.4 Industry Impact
From the study, it can be deduced that non-technical sectors such as retail, healthcare, and finance can be able to use causal inference to solve customer experience, maximize ad spend, and improve decision-making. With machine learning and causal analysis, businesses are in a position to develop customer-centric, data-driven strategies to be successful over the long term. The research sets a strong foundation to the future of marketing analytics technology that is directed towards causal understanding rather than correlational data, thus leading to more productive and effective marketing expenditure.

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