Optimal Design of Concentric Circular Antenna Array Using Particle Swarm Optimization with Constriction Factor Approach

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ABSTRACT

In this paper the maximum sidelobe level (SLL) reductions without and with central element feeding in various designs of three-ring concentric circular antenna arrays (CCAA) are examined using Particle Swarm Optimization with Constriction Factor Approach (PSOCFA) to finally determine the global optimal CCAA design. Binary coded Genetic Algorithm (BGA) is also employed for comparative optimization but it proves to be suboptimal. The present paper assumes non-uniform excitations and uniform spacing of excitation elements in each three-ring CCAA design. Among the various CCAA designs, the three-ring CCAA containing central element and 4, 6 and 8 elements in three successive concentric rings proves to be such global optimal design with global minimum SLL (-17.42dB) determined by PSOCFA.

Categories and Subject Descriptors

B.8.2 [PERFORMANCE AND RELIABILITY]: Performance Analysis and Design Aids

General Terms

Algorithms, Design, Theory

Keywords

Concentric Circular Antenna Array; Non-uniform Excitation; Sidelobe Level; Binary Coded Genetic Algorithm; Particle swarm optimization with constriction factor approach.

1. INTRODUCTION

An antenna array consists of multiple stationary antenna elements, which are often fed coherently. There is abundant open technical literatures [1-6], bearing a common target - bridging the gap between desired radiation pattern having nil SLL with what is practically achievable. The primary method in all these research works is improvement of array pattern by manipulating the structural geometry to suppress the SLL while preserving the gain of the main beam.

Among the different types of antenna arrays, CCAA [1, 5] have become most popular in mobile and wireless communications. In this paper optimization of CCAA design having uniform interelement separations and non-uniform excitations is performed with the help of a novel evolutionary optimization technique.

In this paper the array factors due to non-uniform excitation in various CCAA design structures are examined to find the best possible design structure using two evolutionary techniques, BGA [4] and PSOCFA [7, 8]. Regarding the comparative effectiveness of the techniques, the newly proposed PSOCFA technique proves to be better in attaining minimum SLL, reduction of major lobe beamwidth and hence minimum "Misfitness" objective function values in the optimization of various CCAA designs.

The rest of the paper is arranged as follows: In section 2, the general design equations for the non-uniformly excited CCAA are stated. Then, in section 3, brief introductions for RGA and PSOCFA are presented. Numerical results are presented in section 4. Finally the paper concludes with a summary of the work in section 5.

2. DESIGN EQUATION

Geometrical configuration is a key factor in the design process of an antenna array. For CCAA, the elements are arranged in such a way that all antenna elements are placed in multiple concentric circular rings, which differ in radii and in number of elements. Fig. 1 shows the general configuration of CCAA with M concentric circular rings, where the m^{th} (m=1,2,...,M) ring has a radius r_m and the corresponding number of elements is N_m . If all the elements in all the rings are assumed to be isotopic sources, then the radiation pattern of this array can be written in terms of its array factor only.

Referring to Fig.1, the array factor, $AF(\phi, I)$ for the CCAA in x-y plane is expressed as:

$$AF(\phi, I) = \sum_{m=1}^{M} \sum_{i=1}^{N_{m}} I_{mi} \exp \left[j \left(Kr_{m} \sin \theta \cos (\phi - \phi_{mi}) + \alpha_{mi} \right) \right]$$

(1)

where $I_{\scriptscriptstyle mi}$ denotes current excitation of the $i^{\rm th}$ element of the $m^{\rm th}$ ring. $K=2\pi/\lambda$, λ being the signal wave-length. θ and ϕ symbolize the zenith angle from the positive z axis and the azimuth angle from the positive x axis to the orthogonal projection of the observation point respectively. It may be noted that if the elevation angle is assumed to be 90 degrees i.e. $\theta=90^{\circ}$ then (1) may be written as a periodic function of ϕ with a period of 2π radian. The angle $\phi_{\scriptscriptstyle mi}$ is nothing but element to element angular separation measured from the positive x-axis.

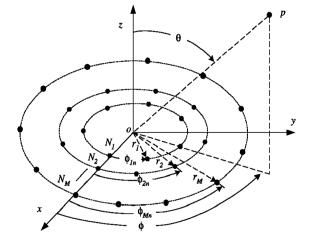


Figure 1. Concentric circular antenna array (CCAA).

As the elements in each ring are assumed to be uniformly distributed, we have,

$$\phi_{mi} = 2\pi \left(\frac{i-1}{N_m}\right); \qquad m = 1, \dots, M; \quad i = 1, \dots, N_m$$
 (2)

 α_{mi} is the phase difference between the individual elements in the array, α_{mi} may be written as:

$$\alpha_{mi} = -Kr_{mi}\cos(\phi_{0} - \phi_{mi}); \quad m = 1, \dots, M; \quad i = 1, \dots, N_{mi}$$
(3)

where ϕ_0 is the value of ϕ where peak of the main lobe is obtained.

After defining the array factor, the next step in the design process is to formulate the objective function which is to be minimized. The objective function "Misfitness" (MF) may be written as (4):

$$\begin{split} MF &= W_{F1} \times \frac{\left| AF\left(\phi_{msl1}, I_{ml}\right) + AF\left(\phi_{msl2}, I_{ml}\right) \right|}{\left| AF\left(\phi_{0}, I_{ml}\right) \right|} \\ &+ W_{F2} \times \left(BWFN_{computed} - BWFN\left(I_{ml} = 1\right) \right) \end{split} \tag{4}$$

BWFN is an abbreviated form of first null beamwidth, or, in simple terms, angular width between the first nulls on either side of the main beam. MF is computed only if $BWFN = \langle BWFN (I=1) \rangle$ and corresponding solution of current excitation weights is retained in the active population otherwise not retained. W_{F1} and W_{F2} are the weighting factors. ϕ_0 is the angle where the highest maximum of central lobe is attained in $\phi \in [-\pi, \pi]$. ϕ_{msl_1} is the angle where the maximum sidelobe $AF(\phi_{msl_2}, I_{msl_2})$ is attained in the lower band and ϕ_{msl_2} is the angle where the maximum sidelobe $AF(\phi_{msl_2}, I_{msl_2})$ is attained in the upper band. W_{F1} and W_{F2} are so chosen that optimization of SLL remains more dominant than optimization of BWFN computed and MF never becomes negative.

In (4) the two beamwidths, $BWFN_{computed}$ and BWFN(I = 1) basically refer to the computed first null beamwidth in radian for

the non-uniform excitation case and for uniform excitation case respectively. Minimization of MF means maximum reductions of SLL both in lower and upper bands and lesser $BWFN_{computed}$

as compared to $BWFN (I_{--} = 1)$. The evolutionary optimization techniques employed for optimizing the current excitation weights resulting in the minimization of MF and hence reductions in both SLL and BWFN are described in the next section.

3. EVOLUTIONARY TECHNIQUES EMPLOYED

3.1 Binary coded Genetic Algorithm (BGA)

GA is mainly a probabilistic search technique, based on the principles and concept of natural selection and evolution. At each generation it maintains a population of individuals where each individual is a coded form of a possible solution of the problem at hand and called chromosome. Chromosomes are constructed over some particular alphabet, e.g., the binary alphabet [0, 1], so that chromosomes' values are uniquely mapped onto the decision variable domain. Each chromosome is evaluated by a function known as fitness function, which is usually the cost function or the objective function of the corresponding optimization problem.

Steps of BGA as implemented for the optimization of current excitation weights are:

- Initialization of binary chromosome strings of n_p population, each consisting of a set of excitations.
 Size of the set depends on the number of excitation elements in a particular CCAA design
- Decoding of strings and evaluation of "Misfitness"
 (MF) of each string
- Selection of elite strings in order of increasing (MF) values from the minimum value
- Copying of the elite strings over the non-selected strings
- Crossover and mutation to generate off-springs.
- Genetic cycle updating
- The genetic cycle stops when the maximum number of generations is reached. The grand minimum
 (MF) and its corresponding chromosome string or the desired solution are finally obtained.

3.2 Particle Swarm Optimization (PSO)

PSO is a flexible, robust population-based stochastic search/optimization technique with implicit parallelism, which can easily handle with non-differential objective functions, unlike traditional optimization methods. PSO is less susceptible to getting trapped on local optima unlike GA, Simulated

Annealing etc. Eberhart and Shi [7] developed PSO concept similar to the behavior of a swarm of birds. PSO is developed through simulation of bird flocking in multidimensional space. Bird flocking optimizes a certain objective function. Each agent knows its best value so far (pbest). This information corresponds to personal experiences of each agent. Moreover, each agent knows the best value so far in the group (gbest) among pbests. Namely, each agent tries to modify its position using the following information:

- The distance between the current position and pbest.
- The distance between the current position and gbest.

Mathematically, velocities of the particles are modified according to the following equation:

$$V_{i}^{t+t} = w * V_{i}^{t} + C_{i} * rand_{i} * (pbest_{i}^{t} - S_{i}^{t}) + C_{2} * rand_{2} * (gbest_{i}^{t} - S_{i}^{t})$$
(5)

where V_i^k is the velocity of agent i at iteration k; w is the weighting function; C_j is the weighting factor; rand is the random number between 0 and 1; S_i^k is the current position of agent i at iteration k; $pbest_i^k$ is the pbest of agent i; $gbest^k$ is the gbest of the group. The searching point in the solution space can be modified by the following equation:

$$S_i^{k+1} = S_i^k + V_i^{k+1} (6)$$

The first term of (5) is the previous velocity of the agent. The second and third terms are used to change the velocity of the agent. Without the second and third terms, the agent will keep on "flying" in the same direction until it hits the boundary. Namely, it corresponds to a kind of inertia and tries to explore new areas. The values of w, C_1 and C_2 are given in the next section.

3.2.1 Particle swarm optimization with constriction factor approach (PSOCFA):

For PSOCFIWA, the velocity of (5) is manipulated in accordance with (7).

$$V_{I}^{k+1} = CF \times (V_{I}^{k} + C_{1} * rand_{1} * (pbest_{I} - S_{I}^{k}) + C_{1} * rand_{1} * (gbest - S_{I}^{k}))$$

$$(7)$$

Normally, C_1 = C_2 =1.5-2.05 and constriction factor (CF) varies from 0.6-0.73. The best values of C_1 , C_2 , and CF are found to vary with the design sets. The solution updating is same as (6).

4. EXPERIMENTAL RESULTS

This section gives the experimental results for various CCAA designs obtained by BGA and PSOCFA techniques. For each optimization technique ten three-ring (M=3) CCAA structures for two cases as a) without central element feeding and b) with central element feeding in three-ring concentric circular antenna arrays (CCAA) are assumed. Each CCAA maintains a fixed spacing between the elements in each ring (inter-element spacing being 0.55λ , 0.61λ and 0.75λ for first ring, second ring and third ring respectively). These spacings are the means of the values determined for the ten structures for non-uniform spacing and

non-uniform excitations in each ring using 25 trial generalized optimization runs for each structure. This generalized optimization is beyond the scope of this paper. For all sets of experiments, the number of elements of the inner most circle is N_1 , for outermost circle is N_3 , whereas the middle circle consist of N_2 number of elements. For all the cases, $\phi_0 = 0^0$ is considered so that the centre of the main lobe in radiation patterns of CCAA starts from the origin. After experimentation, best proven values of W_{F1} and W_{F2} are fixed as 18 and 1 respectively.

The following best proven parameters for the BGA and PSOCFA are i) Initial population = 120 chromosomes, ii) Maximum number of iteration cycles = 800 (BGA), 80 (PSOCFA); lesser number of cycles is found to be sufficient for the convergences of PSOCFA, since PSOCFA's convergence rate is higher than BGA's convergence rate, iii) For BGA, Selection probability, Crossover (dual point) ratio and mutation probability = 0.3, 0.8 and 0.004 respectively, iv) For PSOCFA, C1 = C2 = 1.5, CF = 0.65, are the best proven values of the parameters.

Table 1. SLL and BWFN for uniformly excited (I_{mi} =1) CCAA sets

Set No.	No. of elements in each rings (N ₁ ,N ₂ ,N ₃)	central	hout element e (a))	With central element (Case (b))	
		SLL (dB)	BWF N (deg)	SLL (dB)	BWF N (deg)
I	2, 4, 6	-6.28	128.4	-8.5	140.0
II	3, 5, 7	-6.89	107.2	-7.5	116
Ш	4, 6, 8	-5.6	90.3	-6.16	95.4
IV	5, 7, 9	-5.6	78.2	-6.62	81.6
V	6, 8, 10	-5.17	68.4	-6.0	71.1
VI	7, 9, 11	-5.0	61.0	-5.66	63.0
VII	8, 10, 12	-4.78	54.8	-5.38	56.4
VIII	9, 11, 13	-4.64	50.0	-5.17	51.3
IX	10, 12, 14	-4.53	46.0	-5.0	47.0
X	11, 13, 15	-4.45	42.0	-4.88	43.2

Each BGA and PSOCFA generates a set of normalized non-uniform current excitation weights for all sets of CCAA. I_{mi} =1 corresponds to uniform current excitation. Partial results for BGA and PSOCFA are shown in Tables 2-5. Table 1 depicts SLL values and BWFN values for all corresponding CCAA structures

Table 2. Current excitation weights, SLL and BWFN for non-uniformly excited CCAA sets (Case (a)) using BGA

Set	Current excitation weights	SLL	BWF
No.	for the array elements	(dB)	N
	$(I_{11}, I_{12},, I_{mi})$, ,	(deg)
III	1.0000 0.9450 0.7463 1.0000 0.6799 0.7126 1.0000 0.6068 0.6864 1.0000 0.6021 1.0000 0.6803 0.2289 0.6721 0.8732 0.5849 0.1872	-13.07	73.6
V	0.9219 0.7227 0.8711 0.5781 0.5352 0.9805 0.9922 0.2500 0.8438 0.6094 0.5898 0.2539 0.5977 0.8984 0.1523 0.8672 0.8086 0.2461 0.4844 0.4414 0.5000 0.4883 0.8750 0.5313	-10.81	60.4
VII	0.5898 0.5078 0.8164 0.9492 0.7227 0.3711 0.8086 0.9922 0.6875 0.1055 0.0742 0.6055 0.4570 0.9063 0.1836 0.2656 0.6211 0.5391 0.5938 0.4531 0.8711 0.5000 0.5469 0.5117 0.2461 0.4961 0.9570 0.429 0.2422 0.4570	-12.0	49.5

Table 3. Current excitation weights, SLL and BWFN for nonuniformly excited CCAA sets (Case (b)) using BGA

Set No.	Current excitation weights for the array elements $(I_{11}, I_{12},, I_{mi})$	SLL (dB)	BWF N (deg)
III	0.3789 0.7344 0.9766 0.8164 0.9922 0.7148 0.5508 0.9727 0.7969 0.9102 0.9805 0.6680 0.8750 0.6523 0.1406 0.6406 0.9063 0.5508 0.1680	-14.53	78.3
V	0.4961 0.7500 0.4375 0.7422 0.7891 0.4219 0.4961 0.5703 0.1719 0.7344 0.7461 0.5117 0.5000 0.4492 0.7969 0.1992 0.6797 0.7109 0.4648 0.3203 0.3008 0.8125 0.6055 0.3438	-11.67	57.9
VII	0.4570 0.5625 0.8359 0.6328 0.9961 0.8633 0.7969 0.7734 0.9805 0.5000 0.2500 0.1641 0.8398 0.2422 0.8750 0 0.0781 0.8750 0.4258 0.5234 0.1094 0.8711 0.3828 0.2148	-12.96	51.6

4.1 Analysis of Radiation Pattern of Optimal CCAA

Figs. 2-3 depict the substantial reductions in SLL with nonuniform optimal current excitations as compared to the case of uniform non-optimal current excitations. All CCAA sets having central element feeding (Case (b)) yield much more reductions in SLL as compared to the same not having central element feeding (Case (a)). As seen from Tables 2-5, SLL reduces to -13.07dB (BGA), - 16.65dB (PSOCFA) for Case (a) and -14.53dB (BGA), -17.42dB (grand highest SLL reduction as determined by PSOCFA) for Case (b) with the CCAA set having N₁=4, N₂=6, N₃=8. This optimal set along with central element feeding yields grand maximum SLL reductions for both techniques among all the sets. BWFN become narrower for non-uniform optimal current excitation weights as compared to the uniform nonoptimal excitations for all sets in both the test cases. For the same optimal CCAA set, the BWFN values are 73.60 (RGA) and 77.1⁰ (PSOCFA) for Case (a), 78.3⁰ (RGA) and 82.7⁰ (PSOCFA) for Case (b) against 90.3° (Case (a)), 95.4° (Case (b)) for the corresponding uniformly excited CCAA having the same number of elements.

So, these techniques yield maximum reductions of BWFN also for this optimal CCAA (shown as shaded rows in the Tables 2-5). The programming is written in MATLAB 7.5 version on core (TM) 2 duo processor, 3.00 GHz with 2 GB RAM.

Table 4. Current excitation weights, SLL and BWFN for nonuniformly excited CCAA sets (Case (a)) using PSOCFA

Set	Current excitation weights for				SLL	BWF	
No.	the array elements				(dB)	N	
	$(I_{11}, I_{12},, I_{mi})$					(deg)	
		11, 112	, , , , , , _{mi})			(=====)	
III	0.0831	0.6696	0.0821	0.6210	-16.65	77.1	
	0.3860	0.4254	0.9383	0.3955			
	0.3907	1.0000	0.4938	0.6647			
	0.4536	0.2223	0.4496	0.6664			
	0.4867	0.2533					
V	1.0000	0.6626	0.8101	0.4564	-12.55	60.6	
	0.5287	1.0000	0.8774	0			
	0.8663	0.7790	0.6590	0			
	1.0000	0.8367	0.2976	0.9699			
	1.0000	0.3719	0.5041	0.4080			
	0.4853	0.7283	0.3799	0.3983			
VII	0.8709	0.6058	0.7297	1.0000	-12.7	51.5	
	0.8920	0.5959	1.0000	1.0000			
	0.6442	0	0.1753	0.4793			
	0.3796	1.0000	0	0			
	1.0000	0.3763	0.6032	0.2461			
	1.0000	0.1953	0.5416	0.4483			
	0	0.6097	1.0000	0.5832			
	0.3946	0.4450					

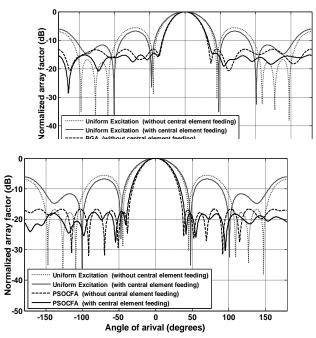


Figure 3. Radiation pattern for a uniformly excited and PSOCFA based non-uniformly excited CCAA (N₁=4, N₂=6, N₃=8 elements).

Table 5. Current excitation weights, SLL and BWFN for nonuniformly excited CCAA sets (Case (b)) using PSOCFA

Set No.	Current excitation weights for the array elements $(I_{11}, I_{12},, I_{mi})$				SLL (dB)	BWF N (deg)
Ш	0.8076	0.7623 0.7689 0.4938	0.6066		<u>-17.42</u>	82.7
V	0.0549 0 1.0000	0.8413 1.0000 0.9236 1.0000 0.9093 1.0000	1.0000 0.4673	0.4329	-13.16	60.0
VII	0.5670	0.7281 1.0000 0.5408 0.4491 1.0000 0.4317	0.5129 0.5432	0.6508 0 0 0.3984 0.3736	-13.68	52.8

5. CONCLUSION

In this paper, the optimal design of a non-uniformly excited CCAA with uniform inter-element spacing and without / with central element feeding has been described using the evolutionary optimization techniques as BGA and PSOCFA. PSOCFA technique proves to be faster and robust technique; yields optimal excitations and global minimum values of SLL and BWFN for all sets of CCAA designs. BGA is less robust and yield suboptimal results. Experimental results reveal that the design of non-uniformly excited CCAA offers a considerable SLL reduction along with the reduction of BWFN as compared to the corresponding uniformly excited CCAA. The main contribution of the paper is threefold: (i) All CCAA having central element feeding yield much more reduction in SLL as compared to the same not having central element feeding, (ii) The CCAA set having $N_1=4$, $N_2=6$, $N_3=8$, with central element feeding gives the grand maximum SLL reduction (-17.42dB) as compared to all other sets, which one is thus the grand optimal set among all the three-ring structures, and iii) Comparing the performance of both techniques PSOCFA shows the better optimization performance as compared to BGA.

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